

## The Bounded Approximation Property for Weakly Uniformly Continuous Type Holomorphic Mappings

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*Abstract:* When  $U$  is a balanced open subset of a reflexive Banach space  $E$  with  $\mathcal{P}({}^n E) = \mathcal{P}_w({}^n E)$  for every positive integer  $n$ , we show that the predual of the space of weakly uniformly continuous holomorphic mappings on  $U$ ,  $G_{wu}(U)$ , has the bounded approximation property if and only if  $E$  has the bounded approximation property if and only if  $\mathcal{P}({}^n E)$  has the bounded approximation property for every positive integer  $n$ . An analogous result is established for the predual of the space of holomorphic mappings of bounded type also.

*Key words:* Banach spaces, locally convex spaces, bounded approximation property, holomorphic mappings of bounded type, weakly uniformly continuous functions, bounded holomorphic mappings.

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