

Weighted Composition Operators on Weighted Bergman Spaces

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Presented by Fernando Cobos

Received May 4, 2007

Abstract: In this paper, we study boundedness, compactness and the essential norm of a class of weighted composition operators on weighted Bergman spaces.

Key words: Bergman spaces, Carleson measure, essential norm, weighted composition operators.

AMS *Subject Class.* (2000): 47B33, 46E30, 47B07.

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