

## On Derived Categories and Derived Functors

SAMSON SANEBLIDZE

*A. Razmadze Mathematical Institute, Department of Geometry and Topology  
M. Aleksidze st., 1, 0193 Tbilisi, Georgia, sane@rmi.acnet.ge*

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*Abstract:* For an abelian category, a category equivalent to its derived category is constructed by means of specific projective (injective) multicomplexes, the so-called homological resolutions.

*Key words:* derived category, derived functor, multicomplex, homological resolution.

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