

## Weighted Composition Operators Between Besov Spaces

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*Abstract:* In this paper, we study the boundedness, the compactness and the essential norm of weighted composition operators between Besov spaces. We also find estimates for the essential norm of weighted composition operators between  $S^p$  spaces.

*Key words:* Besov spaces, Carleson measure, essential norm,  $S^p$  spaces, weighted composition operators.

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